# Measuring Student's Proficiency in MOOCs: Multiple Attempts Extensions for the Rasch Model 

Dmitry Abbakumov ${ }^{1,2}$, Piet Desmet ${ }^{1}, \&$ Wim Van den Noortgate ${ }^{1}$

${ }^{1} \mathrm{KU}$ Leuven (University of Leuven), Leuven, Belgium

${ }^{2}$ National Research University Higher School of Economics, Moscow, Russia

## MOOCs

A Massive Open Online Course is an online course with (open) access and unlimited participation of students...
... consists of pre-recorded video lectures, reading assignments, assessments, and forums.
$\ldots$ is developed by universities and run on Coursera, edX, XuetangX, FutureLearn, Udacity, MiriadaX.
In 2017, 800 universities offered 9,400 MOOCs. The same year, Coursera
 achieved the milestones of 30 million students and 2,700 courses.

## Context

Students, professors and universities have an interest in accurate student proficiency measuring.

## Problem

Assessments are dynamic: items can be added, removed or replaced by a course author at any time $+$

Students are allowed to make several attempts within one assessment
$+$
Assessments may include an insufficient number of items for accurate individual-level conclusions

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$$

Common psychometric models and techniques of Classical Test Theory (CTT) and Item Response Theory (IRT) do not serve perfectly to measure proficiency


## Framework

The Rasch model

$$
\operatorname{Logit}\left(\pi_{i j} \mid \theta_{j}\right)=\ln \left(\pi_{i j} / 1-\pi_{i j}\right)=\theta_{j}-\delta_{i} \text { and } Y_{i j} \sim \operatorname{Bernoulli}\left(\pi_{i j}\right)
$$

The reformulation presented by Van den Noortgate, De Boeck, \& Meulders (2003)
$\operatorname{Logit}\left(\pi_{i j}\right)=b_{0}+u_{1 j}+u_{2 i}$ and $Y_{i j} \sim \operatorname{Bernoulli}\left(\pi_{i j}\right)$
where $u_{1 j} \sim N\left(0, \sigma_{u 1}^{2}\right)$ and $u_{2 i} \sim N\left(0, \sigma_{u 2}^{2}\right)$
$\rightarrow$ very flexible for making extensions

## Extension One

We consider two components of proficiency within weekly summative assessment: the fixed component and the dynamic component.

$$
\operatorname{Logit}\left(\pi_{i j}\right)=b_{0}+\left(b_{10}+\boldsymbol{b}_{1 j}\right) * \operatorname{attempt}_{i j}+u_{1 j}+u_{2 i} \text { and } Y_{i j} \sim \operatorname{Bernoulli}\left(\pi_{i j}\right)
$$

## Extension Two

The effect of additional attempt may vary from item to item (e.g. the difference between multiple choice and open-ended items)

$$
\operatorname{Logit}\left(\pi_{i j}\right)=b_{0}+\left(b_{10}+b_{1 j}+b_{1 i}\right) * \text { attempt }_{i j}+u_{1 j}+u_{2 i} \text { and } Y_{i j} \sim \operatorname{Bernoulli}\left(\pi_{i j}\right)
$$

## (Explanatory) Extensions Three and Four

We assume the more attempts a student makes, the less his/her effect of attempt (e.g. multiple guessing vs. learning from tips and hints)
$\operatorname{Logit}\left(\pi_{i j}\right)=b_{0}+\left(b_{10}+b_{1 j}+b_{1 i}\right) *$ attempt $_{i j}+b_{2} *$ class $_{j}+b_{3} *$ attempt $_{i j} *$ class $_{j}+u_{1 j}+u_{2 i}$ and $Y_{i j} \sim \operatorname{Bernoulli}\left(\pi_{i j}\right)$

How does the student's activity in the course link to his/her proficiency?

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\(\operatorname{Logit}\left(\pi_{i j}\right)=b_{0}+\left(b_{10}+b_{1 j}+b_{1 i}\right) *\) attempt \(_{i j}+b_{2} *\) class \(_{j}+b_{3} *\) attempt \(_{i j} *\)
class \(_{j}+b_{4} *\) formative.assessment.performance \({ }_{j}+b_{5} *\) lecture.activity \(_{j}+\)
\(u_{1 j}+u_{2 i}\) and \(Y_{i j} \sim \operatorname{Bernoulli}\left(\pi_{i j}\right)\)
```


## Illustration - Data

"Economics for Non-Economists" MOOC on Coursera
$N=1,609$ from Russia (72\%), Ukraine (8.4\%), Kazakhstan (3.9\%), Belarus (3.2\%), USA (1.2\%), other countries (11.3\%)

The weekly summative assessment includes 10 items
51,550 responses
Attempts: $M=2.04$ SD=1.52.

## Illustration - Results

|  |  |  | Basic Mod. | Extension 1 | Extension 2 | Extension 3 | Extension 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fixed | Intercept |  | 0.63 (0.22) | 0.27 (0.25) | 0.29 (0.27) | 0.65 (0.27) | -0.75 (0.30) |
|  | Attempt |  |  | 0.92 (0.03) | 0.90 (0.06) | 1.34 (0.07) | 1.34 (0.07) |
|  | Class |  |  |  |  | -0.48 (0.03) | -0.42 (0.03) |
|  | Attempt * Class |  |  |  |  | -0.33 (0.03) | -0.33 (0.03) |
|  | Lect. Act. |  |  |  |  |  | 0.32 (0.07) |
|  | Pract. Perf. |  |  |  |  |  | 1.16 (0.09) |
|  |  |  | SD | SD | SD | SD | SD |
| Random | Intercept | Student | 0.78 | 0.92 | 0.96 | 0.86 | 0.77 |
|  |  | Item | 1.01 | 1.12 | 1.22 | 1.22 | 1.22 |
|  | Attempt | Student |  | 0.60 | 0.59 | 0.52 | 0.52 |
|  |  | Item |  |  | 0.21 | 0.21 | 0.21 |
| AIC |  |  | 58779 | 55401 | 54929 | 54487 | 54260 |

## Cross-Validation

## 3 MOOCs, 9 assessments with 10-15 items

$N=9,484,>500 \mathrm{~K}$ responses
training/test proportion 75/25, 10 replications

|  | Overall | Course 1 |  |  |  | Course 2 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | M | SD | M | SD | M | SD | M | SD |
| Rasch (1" att.) | .710 | .07 | .695 | .03 | .638 | .02 | .797 | .02 |
| Basic Model | .739 | .06 | .719 | .03 | .688 | .01 | .811 | .02 |
| Extension 1 | .768 | .04 | .751 | .02 | .734 | .02 | .819 | .02 |
| Extension 2 | .770 | .04 | .753 | .02 | .737 | .02 | .820 | .02 |
| Extension 3 | .770 | .04 | .753 | .02 | .737 | .02 | .821 | .02 |
| Extension 4 | .771 | .04 | .754 | .02 | .738 | .02 | .821 | .02 |

Key notes:

- more accurate measures and conclusions on the proficiency
- the transition from analysis of responses to analysis of behavior (in the course)

Limitations and further work:

- peer-assessments and programming assignments

Thank you!

